

## Signal Enhancement and Limiting Factors in Waveguides Containing Si Nanoclusters and Er<sup>3+</sup> Ions

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Rib-loaded waveguides containing Er<sup>3+</sup> ions coupled to Si nanoclusters (Si-nc) prepared by reactive magnetron co-sputtering have been studied with the aim of improving the optical amplification at 1.54  $\mu\text{m}$ . A set of waveguides with different refractive indices has been fabricated by reducing the annealing duration to investigate the influence of the reorganization (quality) of the dielectric matrix and of the Si-nc clustering on the amplification of Er<sup>3+</sup> signal. Insertion losses, photoluminescence, lifetime and pump/probe measurements have been carried out to characterize, understand and optimize the main factors that are preventing a net optical gain in these samples, i.e., low excitable erbium fraction through the nanoclusters, cooperative up-conversion and confined carrier absorption. Evidences of partial inversion of the Er<sup>3+</sup> ions excited via Si-nc are presented. [DOI: 10.1143/JJAP.46.6626]

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### 1. Introduction

Integrated erbium-doped waveguide amplifiers (EDWAs) are fundamental elements in planar lightwave circuits thanks to their compactness and easy of integration on Silicon wafers. A limitation to their diffusion is their cost. One way to overcome the cost is the use of broadband efficient sensitizers for Er<sup>3+</sup> ions such as Si nanoclusters (Si-nc) in SiO<sub>2</sub> which allows substituting expensive pump sources by low cost broad-band excitation lamps. In fact, the pump light is absorbed by the Si-nc which transfer their excitation to the Er<sup>3+</sup> ions. Thus, the effective excitation cross section of the Er<sup>3+</sup> 1.54  $\mu\text{m}$  luminescence ( $\sigma_{\text{exc}}$ ) broadens and strengthens up to values of  $10^{-16} \text{ cm}^2$ , when visible light is used and at low flux.<sup>1–5</sup> These  $\sigma_{\text{exc}}$  values are orders of magnitude larger than those of Er<sup>3+</sup> in SiO<sub>2</sub>, where one measures absorption cross section values of  $10^{-21} \text{ cm}^2$  at  $\lambda_{\text{exc}} = 980 \text{ nm}$ .<sup>6,7</sup> Quantum efficiencies greater than 60% and Si-nc to Er<sup>3+</sup> transfer rates higher than  $1 \mu\text{s}^{-1}$  by pumping at 488 nm have been also measured.<sup>8</sup> In addition to the increase of  $\sigma_{\text{exc}}$ , Si-nc increase the average refractive index of the dielectrics, allowing good light confinement, and conduct electrical current,<sup>9,10</sup> which opens the route to electrically pumped optical amplifiers. Encouraging results about Er<sup>3+</sup> coupled Si-nc optical amplifiers have been reported by Shin *et al.*<sup>11,12</sup> and by us.<sup>13</sup>

In order to engineer the system, with the aim of achieving a net optical gain in the amplifiers, the role of detrimental processes is to be figured out. Indeed, it is likely that processes like cooperative up-conversion (related to the Er content), confined carrier absorption (CA), Auger non radiative de-excitations and excited state absorption (ESA) within the Si-nc prevent net optical gain when reaching high pumping fluxes.<sup>13–15</sup> While in our reactive magnetron co-sputtering prepared samples we have experimental evidences of the presence of the two first processes (cooperative up-conversion and CA), we have not detected measurable fingerprints of the latter ones. In this manuscript we quantify

the importance of the two first mechanisms as a function of the annealing time, having fixed the other processing parameters.

The Er content in the active layer of the waveguide amplifier should be high enough to have large gain still remaining below a threshold value to prevent the occurrence of clustering and cooperative up-conversion phenomena.<sup>15–17</sup> Er<sup>3+</sup> concentrations not exceeding  $(2–4) \times 10^{20} \text{ cm}^{-3}$  are suggested.<sup>18,19</sup> In addition, the Si-nc densities and sizes have to be tuned to achieve a high rate of coupling with Er<sup>3+</sup> ions to excite them efficiently, together with low propagation losses and negligible confined carrier absorption in the waveguide. However, the energy transfer mechanism from Si-nc to Er<sup>3+</sup> is still far from being completely understood.<sup>20</sup> In this work quite low values of Si-nc density [ $(1–5) \times 10^{17} \text{ cm}^{-3}$ ] in comparison to the Er<sup>3+</sup> content have been achieved. Consequently, only a small percentage of the erbium population (2–3%) is sensitive to be excited through indirect energy transfer from the excited Si-nc. This fact, although detrimental for the performance of the amplifier, has allowed us to have some insights in the dependence of the coupling constant with the distance of Er<sup>3+</sup> from Si-nc. The experimental consequence of such a behavior is an effective excitation cross section that depends on the photon flux. In this work, we also address this issue for different annealing times.

To complete the study we show in the last part of the manuscript a study of the amplification properties of this set of samples. Positive signal enhancement has been measured; whose values are consistent with what expected from the previous optical characterization. Therefore, although only an inversion factor of about 10% has been achieved for the highest pump fluxes used, most of the enhancement comes from directly excited erbium. A further increase of the Silicon content to increase the Si-nc density by using low annealing times is suggested in order to minimize the power threshold needed to obtain full population inversion.

### 2. Waveguide Fabrication and Experimental Details

Er<sup>3+</sup> doped Si-nc silica waveguides have been prepared

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Table I. Sample parameters: annealing time, Si-excess, Er content, refractive index  $n$  at 632.8 nm, fundamental optical mode confinement factor  $\Gamma$ .

Sample	Annealing time (min)	Si excess (at. %)	Er content ( $\times 10^{20} \text{ cm}^{-3}$ )	$n$	$\Gamma$
B	60	7	$4 \pm 0.1$	1.545	$0.51 \pm 0.02$
C	30	6–7	$5.4 \pm 0.2$	1.516	$0.48 \pm 0.02$
D	10	6–7	$5.4 \pm 0.2$	$1.48 \pm 0.01$	$0.28 \pm 0.03$

by a multi-wafers reactive magnetron co-sputtering of a pure silica target topped with  $\text{Er}_2\text{O}_3$  pellets. The incorporation of Si excess in the film was obtained by mixing the plasma with hydrogen, owing to its ability to reduce the oxygen provided by the silica target. The hydrogen rate (mixed to argon) was kept to 60% while the Si substrates, on which a  $15 \mu\text{m}$  thermal  $\text{SiO}_2$  layer was previously thermally grown, were not intentionally heated. More details on the process can be found elsewhere.<sup>18)</sup> After the deposition of about  $1 \mu\text{m}$  thick Er/silicon rich oxide (SRO) layer, a  $1 \mu\text{m}$  thick  $\text{SiO}_2$  cladding layer has been deposited by sputtering a  $\text{SiO}_2$  target in pure argon plasma. Then the wafers have been annealed, for different times at  $900^\circ\text{C}$  under pure  $\text{N}_2$  flux to activate  $\text{Er}^{3+}$  ions, to induce the precipitation of the Si excess into nanoclusters that are expected to play the role of sensitizers of  $\text{Er}^{3+}$  ions. The annealing temperature was chosen on the basis of previous optimization studies.<sup>18,19)</sup> The annealing duration has been varied between 1 and 240 min: annealing times longer than 60 min have shown no improvement in the optical properties of  $\text{Er}^{3+}$  doped Si-nc systems. This annealing time variation aimed at controlling the Si-nc size. Secondary ion mass spectroscopy (SIMS) and Rutherford backscattering spectroscopy (RBS) have been performed to determine Si and Er content (see Table I). It is worth noting that the total Si excess is roughly the same for all the samples.

Optical lithography and reactive ion etching have been used to define 2–3 cm long rib-loaded waveguides with rib widths ranging between  $3.5$  to  $12 \mu\text{m}$ . It is worth noting here that the very low refractive indices of the 5 and 1 min annealed films result in no light confinement in the  $1500$ – $1600 \text{ nm}$  range. On the contrary, waveguides annealed at 60 min (from now on sample B), 30 min (sample C), and 10 min (sample D) have quite good light confinement: calculated optical confinement factors  $\Gamma$  of the fundamental mode at  $1535 \text{ nm}$  are  $0.51$ ,  $0.48$ , and  $0.28$ , respectively.

The optical confinement factors have been deduced from the layer thickness and the material refractive index measured by using the  $m$ -line technique<sup>21)</sup> at  $633 \text{ nm}$ . These measurements allow also figuring out the Si-nc size as a function of the annealing time. The index of refraction  $n$  of the Si-nc rich oxide layer has an intermediate value between that of Si and that of the surrounding dielectric. A simple estimate of the effective material refractive index can be obtained by the Bruggeman effective medium theory by considering that the film is composed by amorphous Si-nc (annealing at  $900^\circ\text{C}$  is not enough to induce crystallization<sup>5)</sup>) embedded into a matrix of sub-stoichiometric defected silica  $\text{SiO}_x$  (with  $x$  varying between  $1.63$  and  $2$  with increasing the annealing time). The detailed analysis of

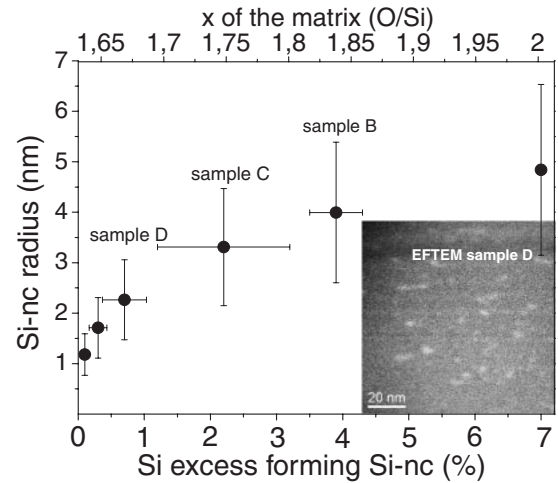


Fig. 1. Radius of Si-nc vs the silicon excess forming Si-nc and TEM micrograph of one of the samples (inset).

this study can be found elsewhere.<sup>22)</sup> It is worth noting here that the refractive index grows as a function of the annealing time (see Table I). From the quantitative analysis we concluded that the substoichiometric matrix becomes close to stoichiometric by increasing the annealing time, precipitating the excess Si into the nanoclusters. Fitting the measured refractive index with the Bruggeman model, the excess Si fraction which precipitates into the Si-nc and the  $x$  of the sub-stoichiometric silica can be inferred. From energy filtered transmission electron microscopy (EFTEM) studies,<sup>23)</sup> a Si-nc density of  $(1-5) \times 10^{17} \text{ cm}^{-3}$  can be estimated for all the samples. Combining this value with the total Si excess that has been precipitated into Si-nc for each annealing time we can estimate the average size of the Si-nc. The results of these estimates are shown in Fig. 1, where it is clear that Si-nc size grows with increasing the Si excess forming Si-nc, i.e., increasing the annealing time. In sample D, for example, the analysis of the Si-nc size distribution determined from the EFTEM images (inset of Fig. 1) shows that the mean radius for this sample is  $1.6 \pm 0.3 \text{ nm}$ , which is actually compatible with the value obtained with our model.

Photoluminescence measurements have been performed by pumping with the  $476 \text{ nm}$  (out of  $\text{Er}^{3+}$  resonance pumping conditions) and  $488 \text{ nm}$  (resonance pumping conditions) lines of an Argon laser and detecting light with a monochromator coupled to an InGaAs photomultiplier. Lifetime measurements were performed using a Ge detector cooled with liquid nitrogen. The laser beam was chopped at  $15 \text{ Hz}$  and its power density was ranging from  $5$  to  $450 \text{ mW cm}^{-2}$ . The overall time response of the experimental setup is about  $0.5 \text{ ms}$ .

Internal gain measurements of the rib-loaded waveguides have been performed by butt-coupling signal light through a single-mode polarization-preserving tapered fiber moved by a piezo-electric stage. The light exiting the end facet of the waveguide was observed with a microscope objective matched, through a prism beam splitter, both to a zoom mounted on an InGaAs camera and to a Ge detector. We have used two different signal light sources: a tunable laser ( $1.5$ – $1.6 \mu\text{m}$ ) that cover the  $^4\text{I}_{13/2} \rightarrow ^4\text{I}_{15/2}$  internal  $\text{Er}^{3+}$

transition (peaked at 1535 nm) and a diode laser operating at 1310 nm, well away from transitions related to  $\text{Er}^{3+}$  ions. The pump source was a Millennia laser (532 nm, 10 W) focused on the waveguide surface onto a stripe 100  $\mu\text{m}$  wide and 1 cm long by means of a cylindrical lens. The alignment of the pump beam and the rib-loaded waveguide was checked by two cameras, which allow observing both the waveguide surface and exit facet. It has to be considered that the pumping wavelength is weakly coupled to an  $\text{Er}^{3+}$  absorption transitions (the absorption cross section at this wavelength is roughly 1/3 of that at 488 nm). Some measurements were done by using the 488 nm line of an Argon laser, resonant with an  $\text{Er}^{3+}$  absorption peak ( $^4\text{I}_{15/2} \rightarrow ^4\text{F}_{7/2}$ ). In order to eliminate the diffused light and the amplified spontaneous emission (ASE) the weak probe signal was chopped (10 kHz) and measured through a lock-in system.

### 3. Emission Cross Sections

The emission cross section  $\sigma_{\text{em}}$  of the  $^4\text{I}_{13/2} \rightarrow ^4\text{I}_{15/2}$  transition of the  $\text{Er}^{3+}$  ions is not significantly enhanced by the presence of the Si-nc and only small differences due to the variation of the effective refractive indices were observed.<sup>24)</sup> Measuring the low pumping rate luminescence spectra,  $\sigma_{\text{em}}(\nu)$  can be obtained in a quantitative manner by using one of the McCumber relations<sup>26)</sup>

$$\sigma_{\text{em}}(\nu) = \sigma_{\text{abs}}(\nu) \exp\left(\frac{\varepsilon - h\nu}{kT}\right), \quad (1)$$

once  $\sigma_{\text{abs}}(\nu)$ , the absorption cross section, is known. In eq. (1),  $\varepsilon$  is the transition energy between the lowest levels of the two  $^4\text{I}_{13/2}$  and  $^4\text{I}_{15/2}$  manifolds,  $T$  the sample temperature, and  $k$  the Boltzmann constant.

$\sigma_{\text{abs}}(\nu)$  has been measured by the insertion loss technique.<sup>13,27)</sup> Absorption losses ( $\alpha_{\text{abs}}$ ) of 7.5, 8.5, and 5.4 dB/cm for samples B, C, and D, respectively, have been measured at 1535 nm.<sup>24)</sup> Then  $\sigma_{\text{abs}}(\nu) = \alpha_{\text{abs}}(\nu)/\Gamma N_{\text{Er}}$ , where  $N_{\text{Er}}$  is the  $\text{Er}^{3+}$  concentration.<sup>28)</sup> From eq. (1),  $\sigma_{\text{em}}(\nu)$  is obtained (Fig. 2). It is observed that decreasing the annealing time,  $\sigma_{\text{em}}(\nu)$  narrows and strengthens, contrary to what expected due to the refractive index decrease since  $\sigma_{\text{em}}(\nu)$  is roughly proportional to the refractive index.<sup>29)</sup> Actually the emission cross section of sample D is almost twice that of sample B. These behaviors are mainly due to the evolution

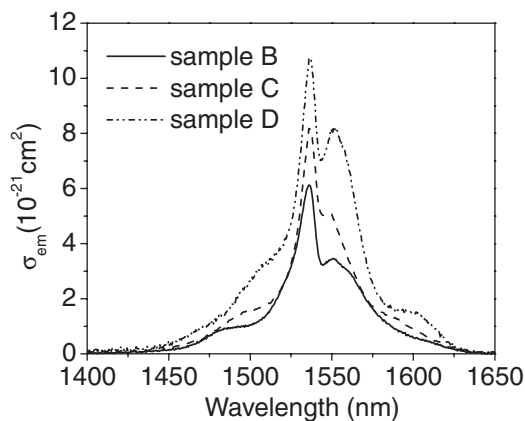


Fig. 2. Emission cross sections calculated from PL spectra at low pump power for samples B (solid line), C (dashed line), and D (dash and dots).

of the local  $\text{Er}^{3+}$  environment with the annealing duration which is changing from a defected  $\text{SiO}_x$  where small Si-nc clusters are present to a two phase Si-nc and  $\text{SiO}_2$  system.<sup>24)</sup> The influence of the local field on the erbium level structure is clearly evidenced when comparing the spectral shapes for the different samples. If only medium fields were involved, no spectral shape change will be observed. The longer the annealing time, the more erbium ions behave as in a pure silica glass (without Si-nc).

### 4. Lifetime Measurements

Luminescence decay measurements at 1535 nm have been performed as a function of the photon flux,  $\Phi$ . The  $\text{Er}^{3+}$  lifetime at low photon flux increases with annealing time (from 1.9 ms for sample D to 3.8 ms for sample B) whereas  $\sigma_{\text{em}}$  decreases (Fig. 2). As already reported, the radiative lifetime increases when the annealing time increases,<sup>24)</sup> but this effect is not enough to explain such a strong increase of the total lifetime. In fact, the probability of having non-radiative recombination increases with decreasing the annealing time for the three studied samples.<sup>24)</sup> At low pump fluxes ( $10^{16}$ – $10^{17}$  photons  $\text{cm}^{-2} \text{s}^{-1}$ ) the temporal decay of the PL signal is well fitted by a single exponential law, which allows associating the behavior of the non-radiative lifetime to recombinations with defects or to concentration quenching effects between excited and non-excited  $\text{Er}^{3+}$  ions. It is worth noting that the probability of having this kind of recombinations is found to be independent of the excited  $\text{Er}^{3+}$  and of the pump photon flux. By increasing the pump flux, cooperative up-conversion recombination between close excited  $\text{Er}^{3+}$  ion pairs starts to play an important role among the other non-radiative recombination paths.

To figure out the role of the different de-excitation mechanism, we have modeled the photoluminescence decay by solving the differential equation that rules the decay rate of the excited level of the  $\text{Er}^{3+}$  population ( $N_2$ ) taking into account specifically the cooperative up-conversion:

$$\frac{dN_2(t)}{dt} = -\frac{N_2(t)}{\tau_d} - C_{\text{up}}N_2(t)^2, \quad (2)$$

where  $\tau_d$  is the lifetime, which counts for the radiative and the  $N_2$  independent non-radiative recombination paths, and  $C_{\text{up}}$  is the up-conversion coefficient between pairs of excited ions.

Aiming at extracting these last two parameters it is necessary to know the initial excited state population for each pump photon flux. Thus, quantitative measurements of the photon flux emitted from the samples were performed by using a reference sample whose emission has been independently evaluated and quantified.<sup>23)</sup> It is so possible to correlate the number of emitted photons to the population of the excited level.

In Fig. 3, the temporal dependence of  $N_2$  for the various samples is reported starting from the steady state population generated at a pump photon flux of  $1 \times 10^{20}$  photons  $\text{cm}^{-2} \text{s}^{-1}$ . We have been able to fit the set of experimental  $N_2$  decays obtained for different pump fluxes by using eq. (2) with fixed values  $\tau_d$  and  $C_{\text{up}}$ . The extracted parameters are shown in the inset of Fig. 3: up-conversion is quite strong in sample D, weak in sample C and even weaker in sample B. We think that this decreasing of the

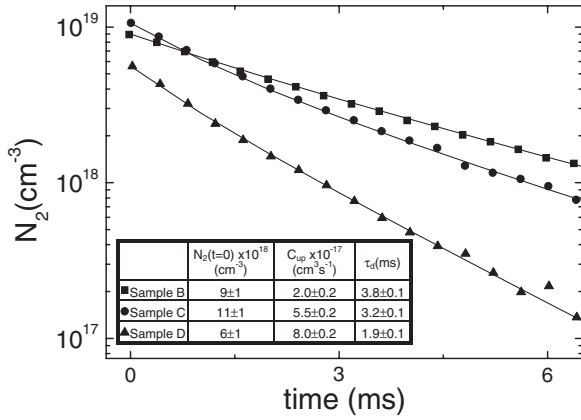


Fig. 3. Temporal behavior of the excited state  $\text{Er}^{3+}$  population  $N_2$ , starting from the steady population obtained at a photon flux of  $10^{20}$   $\text{photon cm}^{-2} \text{s}^{-1}$ . With this photon flux the decays are no more pure exponential due to cooperative up-conversion. The inset shows the parameters extracted from the fitting of the experimental data.

cooperative up-conversion strength is related with the improvement of the matrix when increasing the annealing time.

### 5. Effective Excitation Cross Sections

From time resolved luminescence measurements it is also possible to extract the effective excitation cross section,  $\sigma_{exc}$ , of the  $\text{Er}^{3+}$  ions. In fact, for low pump photon flux,  $\Phi \sim 10^{16} - 10^{17}$   $\text{photons cm}^{-2} \text{s}^{-1}$ , the difference between the reciprocals of the luminescence rise time ( $\tau_r$ ) and decay time ( $\tau_d$ ) can be expressed by:<sup>7)</sup>

$$\frac{1}{\tau_r} - \frac{1}{\tau_d} = \sigma_{exc} \Phi, \quad (3)$$

Figure 4 reports the left part of eq. (3) as a function of the pump photon flux  $\Phi$  for samples B, C, and D excited by resonant (488 nm) and non-resonant (476 nm) wavelengths. A single  $\sigma_{exc}$  value is not able to fit the data. If we want to keep the simple (3), we have to divide the data in two  $\Phi$  regions and use two different  $\sigma_{exc}$  values for  $\Phi \approx 10^{16}$  to  $10^{17}$  and  $10^{17}$  to  $10^{18}$   $\text{photons cm}^{-2} \text{s}^{-1}$ . The results of the fits are reported in Fig. 4. We observe that:

- i) for all the samples,  $\sigma_{exc}$  are orders of magnitude higher than those typical of  $\text{Er}^{3+}$  in pure silica ( $\sim 10^{-21} \text{ cm}^2$ ), which is a consequence of the  $\text{Er}^{3+}$  excitation via the Si-nc;
- ii) the slope is changing with increasing pump photon flux  $\Phi$ , which means that  $\sigma_{exc}$  depends on  $\Phi$ . This effect will be discussed in the following;
- iii) for samples B and C, resonant (488 nm) and non-resonant (476 nm) excitation wavelengths result in the same  $\sigma_{exc}$ , strongly supporting the sensitizing action of the Si-nc;
- iv) however,  $\sigma_{exc}$  of sample D is surprisingly higher with resonant pumping. Note that the values are higher than those for direct  $\text{Er}^{3+}$  absorption. Similar data were reported in ref. 31 without explanation. Since Si-nc absorption smoothly increases as the wavelength decreases,<sup>30)</sup> at the moment we miss the explanation. The very short annealing time could be involved, since the matrix is rich in defects which could prevent or affect the energy transfer from the Si-nc.

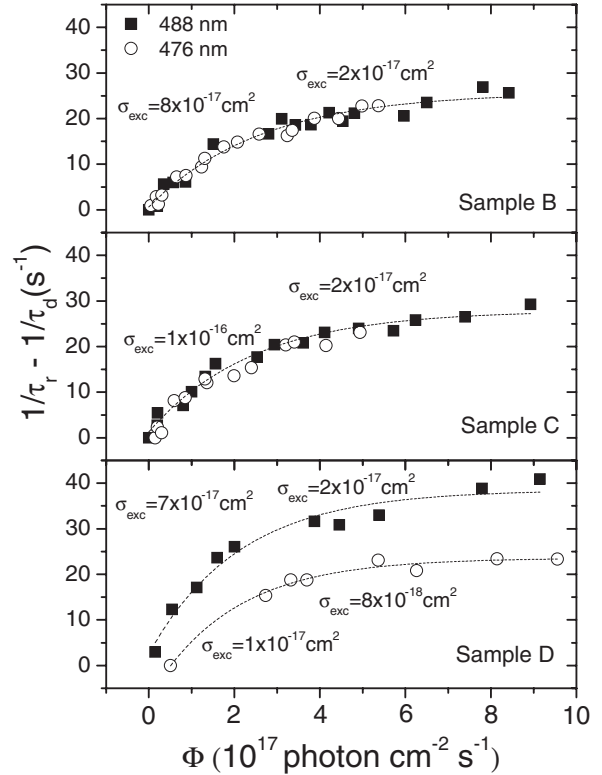


Fig. 4. Difference between the reciprocals of the rise ( $\tau_r$ ) and decay ( $\tau_d$ ) time at low pump flux for 488 nm (solid squares) and 476 nm (empty circles) pumping. The slopes of the curves give  $\sigma_{exc}$ .

Let us try to explain and model the apparent decrease of the effective  $\sigma_{exc}$  with  $\Phi$ . In order to find the more appropriate model we have fitted with the same set of equations and parameters both the lifetime data as a function of the flux for low pump photon fluxes (Fig. 4, top panel) and the excited  $\text{Er}^{3+}$  population obtained from PL measurements for higher fluxes (Fig. 5, open circles). We focus on the results of sample B for the sake of clearness. The model should be able to explain the results of these two different measurements at two completely different pump flux regimes.

Let us briefly describe the model. The exciton population within the Si-nc generated by the pump light can be expressed by the following rate equation:

$$\frac{dN_{Si}^*}{dt} = \sigma_{Si} \Phi (N_{Si} - N_{Si}^*) - \frac{N_{Si}^*}{\tau_{Si}} - k_t N_{Si}^* C_{ind} N_{Er}, \quad (4)$$

where  $N_{Si}^*$  is the density of excitons,  $N_{Si}$  is the total density of Si-nc and  $\sigma_{Si}$  is the absorption cross section of the Si-nc at the pumping wavelength. Note also that  $\tau_{Si}$  is the intrinsic lifetime of the exciton that is a combination of radiative and non-radiative contributions.  $k_t$  is the average coupling rate of the fraction  $C_{ind}$  of  $\text{Er}^{3+}$  ions coupled to Si-nc, i.e., we assume that, of the total  $\text{Er}^{3+}$  content  $N_{Er}$ , only a density  $C_{ind} N_{Er}$  is coupled to the Si-nc. It can be argued that within our experimental conditions ( $\Phi \ll 10^{20}$   $\text{photons cm}^{-2} \text{s}^{-1}$  for the excitation cross section measurement), the excitation transfer from Si-nc to  $\text{Er}^{3+}$  is the dominant deexcitation path and, thus, the steady state solution of eq. (4) is:

$$N_{Si}^* = \frac{\sigma_{Si} \Phi N_{Si}}{k_t C_{ind} N_{Er}}. \quad (5)$$

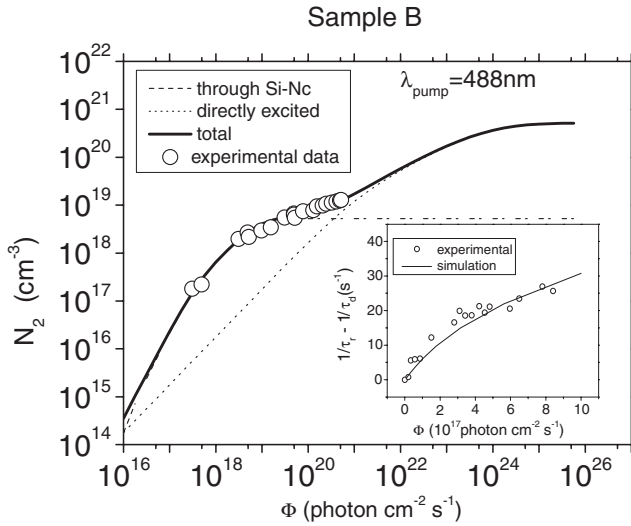


Fig. 5. Sample B: total excited  $\text{Er}^{3+}$  population as a function of pump photon flux as measured (empty circles) and simulated (solid line). The simulated curve is the sum of the directly excited  $\text{Er}^{3+}$  (dotted line) and  $\text{Er}^{3+}$  excited through Si-nc (dashed line). The inset shows the simulated and experimental curves of the difference between the reciprocals of the rise ( $\tau_r$ ) and decay ( $\tau_d$ ) times at low pump flux. The following parameters have been used in the simulations:  $\tau_d = 3.8$  ms,  $C_{\text{up}} = 2 \times 10^{-17}$   $\text{cm}^3 \text{s}^{-1}$ ,  $R_0 = 0.5$  nm,  $\sigma_0 = 3 \times 10^{-16}$   $\text{cm}^2$ ,  $\sigma_d = 5 \times 10^{-21}$   $\text{cm}^2$ ,  $R_{\text{nc}} = 4$  nm.

As for the  $\text{Er}^{3+}$  ions, we assume a two level system to model the rate equations. In fact, other processes that involve higher energy levels are assumed to relax so fast to the second excited level that we can consider the ion as an effective two level system. Auger back transfer to the Si-nc has also been neglected, as it is not a strong recombination path in our material.<sup>32)</sup> We have considered that the equilibrium situation is reached much faster for the exciton population than for the population of the different energy levels of  $\text{Er}^{3+}$ , which means that we can neglect the lifetime of the exciton when it is compared with the lifetime of the  $^4\text{I}_{13/2}$  state of  $\text{Er}^{3+}$ . While only a fraction  $C_{\text{ind}}N_{\text{Er}}$  can be excited through the nanoclusters, the whole  $\text{Er}^{3+}$  population is susceptible to be excited by direct photon absorption, being their excitation cross section  $\sigma_d$ . Moreover, cooperative up-conversion is considered and excited state absorption neglected. Therefore, within our assumptions, the rate equation for the excited level of the  $\text{Er}^{3+}$  ions reduces to:

$$\begin{aligned} \frac{dN_2}{dt} &= KN_{\text{Si}}^*N_1 + \sigma_d\phi N_1 - \frac{N_2}{\tau_d} - C_{\text{up}}N_2^2 \\ &= \sigma_{\text{exc}}\phi N_1 - \frac{N_2}{\tau_d} - C_{\text{up}}N_2^2, \end{aligned} \quad (6)$$

where  $N_1$  is the density of  $\text{Er}^{3+}$  in the ground state,  $N_{\text{Er}} = N_1 + N_2$ . Note that the coupling between the  $\text{Er}^{3+}$  ions and the Si-nc is here described by a coupling rate  $K$  which depends on the particular  $\text{Er}^{3+}$  ion considered, thus  $k_t$  used in eq. (4) is an average of the various  $K$  over the  $\text{Er}^{3+}$  ion coupled population. In eq. (6), we have introduced the effective excitation cross section  $\sigma_{\text{exc}}$  as:

$$\sigma_{\text{exc}} = K \frac{\sigma_{\text{Si}}N_{\text{Si}}}{k_t C_{\text{ind}}N_{\text{Er}}} + \sigma_d. \quad (7)$$

In order to properly fit the data we have considered that the  $\sigma_{\text{exc}}$  of  $\text{Er}^{3+}$  decays with the distance  $R$  from the Si-nc

until it becomes that of the direct excitation  $\sigma_d$ :

$$\sigma_{\text{exc}}(R) = \sigma_0 \exp\left(-\frac{R - R_{\text{nc}}}{R_0}\right) + \sigma_d. \quad (8)$$

Here,  $R_{\text{nc}}$  is the Si-nc radius and  $R_0$  a parameter. This is equivalent to consider a coupling rate  $K$  that decays with the distance.<sup>23)</sup> The picture behind this model is of a system where  $\text{Er}^{3+}$  ions near the Si-nc are efficiently coupled to them, whereas  $\text{Er}^{3+}$  ions far away behave as  $\text{Er}^{3+}$  in  $\text{SiO}_2$  (or in  $\text{SiO}_x$  according to the annealing time and to the simulations shown in Fig. 1). Those last ions can be excited only directly. The rate eq. (6) is then solved for each  $R$  as a function of the pump photon flux. Thus, by integrating over  $R$ , we get the temporal dependence of the total excited state population.

In Fig. 5, we have plotted the experimental data of the excited state population as a function of the pump flux. There are also represented the simulations of the  $\text{Er}^{3+}$  population excited through nanoclusters and directly. The superposition of these two curves reproduces quite well the experimental data. Using the same parameters, we have also reproduced the difference between the reciprocals of the rise and decay times for low  $\Phi$  (inset of Fig. 5). In order to fit both the sets of data (lifetime for low pump fluxes and PL measurements for higher fluxes) we had to assume that only 2–3% of the total  $\text{Er}^{3+}$  population is coupled to the Si-nc, that the typical interaction distance is  $R_0 \sim 0.5$  nm and that  $\sigma_0$  is  $\sim 10^{-16}$   $\text{cm}^2$ . These numbers mean that a large volume percentage of the material is indeed occupied by  $\text{Er}^{3+}$  ions that are too far from a Si-nc and, thus, they are not able to be excited through indirect transfer but through direct photon absorption. The low percentage of  $\text{Er}^{3+}$  excitable through the Si-nc is the most pressing issue for the moment as it hugely reduces the possible performances of the material as an active material.

Equation (8) explains also the observation of Fig. 4: as one increases  $\Phi$ , the  $\text{Er}^{3+}$  coupled to Si-nc are saturated and the excitation of more distant  $\text{Er}^{3+}$  ions is now occurring directly which translates into a decrease of  $\sigma_{\text{exc}}$ . Saturation is due to the ms lifetime of  $\text{Er}^{3+}$  compared to the  $\mu\text{s}$  transfer time from Si-nc to  $\text{Er}^{3+}$ . A detailed modeling addressing this problem is the subject of another letter.<sup>23)</sup> It is also worth noting that a combination of this model together with a flux dependent coupling constant (due to excited state absorption or Auger back transfer) can also lead to a good reproducibility of the experimental results.

## 6. Signal Enhancement

Since we are interested in a waveguide amplifier, we performed amplification studies. What we measured is the signal enhancement factor SE, which is equal to the ratio of the transmitted signal intensity when the waveguide is excited, i.e., under pumping  $I_{\text{pp}}$ , to the transmitted signal intensity when the waveguide is not excited, i.e., without pump ( $I_{\text{p}}$ ). To model  $SE = I_{\text{pp}}/I_{\text{p}}$ , we approximate the system as a two level system and we work in the regime of weak probes,<sup>34)</sup> then

$$\begin{aligned} SE &= \exp(2\sigma_{\text{em}}N_2L\Gamma) \\ &\approx \exp\left[\left(\frac{2\Phi\sigma_{\text{exc}}}{\frac{1}{\tau_d(\Phi)} + \Phi\sigma_{\text{exc}}}\right)\sigma_{\text{em}}N_{\text{Er}}L\Gamma\right], \end{aligned} \quad (9)$$

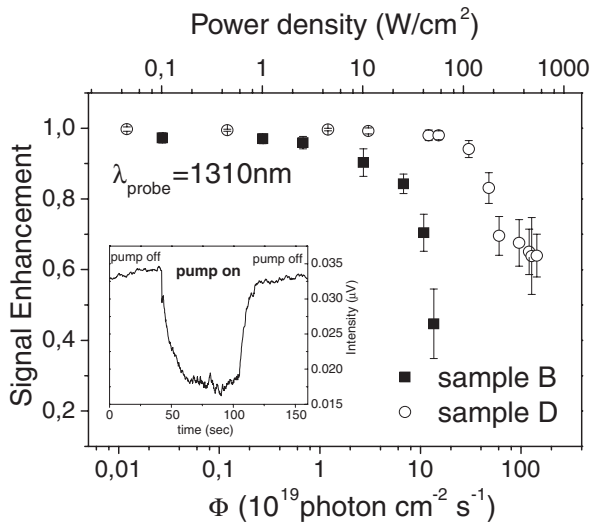


Fig. 6. Signal enhancement as a function of pump photon fluxes (wavelength 532 nm) when using a 1310 nm wavelength probe signal. The inset of the figure shows the time variation of the probe signal when the pump is switched off and on.

where  $L$  is the length of the excited volume. The  $\Phi$  dependence of  $\tau_d$  was already explained in the previous section mainly in terms of cooperative up-conversion mechanisms. It is also worth noting that the internal gain coefficient in  $\text{cm}^{-1}$  will be defined as  $g = \sigma_{em} N_2 \Gamma$ .

Figure 6 reports the signal enhancement at a wavelength of 1310 nm as a function of  $\Phi$ .  $\text{Er}^{3+}$  does not have any absorption resonance at this wavelength. Thus, the decreasing SE is due to a flux-dependent propagation loss mechanism. The most suitable candidate is confined CA within the Si-nc: an absorption mechanism, which depletes the Si-nc excited population and, as a consequence, introduces a new loss mechanism for the signal light and turns off the excitation of  $\text{Er}^{3+}$  via Si-nc.<sup>13)</sup> When decreasing the annealing time, this detrimental CA process is decreased. In fact,  $SE = 0.7$  for  $\Phi = 1 \times 10^{20}$  photons  $\text{cm}^{-2} \text{s}^{-1}$  for sample B while  $SE = 0.7$  for  $\Phi = 6 \times 10^{20}$  photons  $\text{cm}^{-2} \text{s}^{-1}$  for sample D. Sample C showed a similar behavior to what observed in sample D. In ref. 13, we used a resonant pump wavelength of 488 nm, and found a lower CA contribution. These two experimental evidences support the attribution of the  $\Phi$ -dependent losses to CA. Indeed CA decreases when the Si-nc sizes decreases and CA increases quadratically with  $\Phi$ . The inset of Fig. 6 shows the time dependence of SE: it has long turn-on and turn-off times. These long times cannot be explained by the lifetime of excitons in Si-nc, which are of the order of tens of microseconds. As suggested in ref. 8, these long lifetimes can be attributed to excitons, which are formed by electrons and holes excited in nearby Si-nc and thus separated by a large distance. It has been recently observed by Forcales *et al.*<sup>24)</sup> similar long lifetime behaviors on ion implanted samples, explained in terms of the presence of specific charge traps within nanoclusters or damaged nanocrystals.

When using a signal wavelength of 1535 nm, we are probing the  $\text{Er}^{3+}$  absorption band maximum. Figure 7 shows the measured SE as a function of  $\Phi$  while the inset of the figure shows the temporal behavior of the probe when the

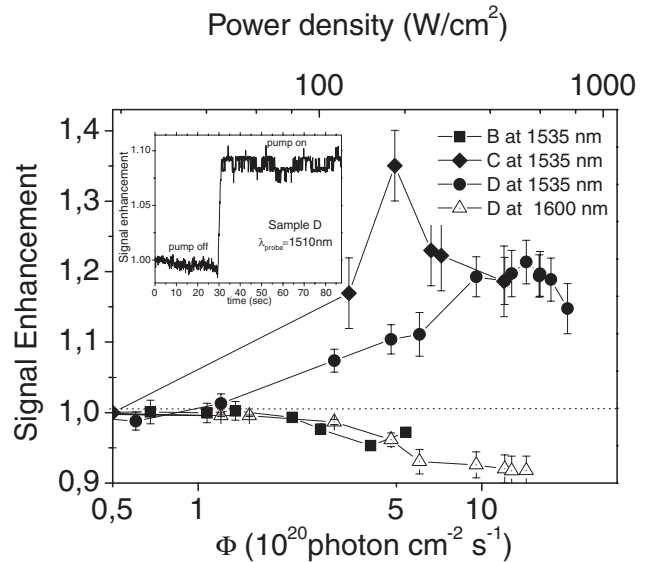


Fig. 7. Signal enhancement using a 1535 nm wavelength probe signal for samples B (squares), C (diamonds), and D (circles). Empty triangles are the signal enhancement at a probe wavelength of 1600 nm. The pump wavelength was 532 nm for samples B and D and 488 nm for sample C. The inset shows the time variation of the probe signal when the pump is switched off and on.

pump is switched on. SE for sample B is weakly below 1: pump induced absorption is present. However, as we increase the pump rate a weak increase of SE is observed. This behavior has been already discussed in ref. 13 as due to two competing mechanisms: CA in the Si-nc and amplification due to direct pumping of the  $\text{Er}^{3+}$  ions. Instead, in samples C and D,  $SE > 1$  and reaches a maximum of 1.35 (0.65 dB/cm) and 1.22 (0.43 dB/cm) respectively at a power density of few hundreds of  $\text{W cm}^{-2}$ . This internal gain is due to indirect excited  $\text{Er}^{3+}$ . For higher pump power, two competing mechanisms act on the Si-nc: energy transfer to the  $\text{Er}^{3+}$  and CA. Let us concentrate on CA. Once a Si-nc is excited, it is prone to absorb a signal photon. This process on one side increases the losses at the signal photon wavelength, on the other side depletes the Si-nc excitation. As a consequence, the effective excitation cross section of  $\text{Er}^{3+}$  decreases and the propagation losses at the signal wavelength increase. This is what one can readily see in Fig. 7: at high  $\Phi$ , SE decreases in both samples. Note that in ref. 13 for sample B we were able to achieve a maximum  $SE = 1.06$  (0.12 dB/cm) at one order of magnitude higher photon flux while pumping at 488 nm, i.e., resonantly with an  $\text{Er}^{3+}$  absorption band.

A rough data analysis allows correcting the SE data from the CA losses; we have divided the SE data at 1535 nm by the SE measured at 1600 nm, where the emission of  $\text{Er}^{3+}$  is quite low. As a result, we obtain a maximum SE of 1.42 (1.52 dB/cm) and 1.30 (1.12 dB/cm) for samples C and D respectively, that translates in an internal gain of 0.76 dB/cm ( $0.18 \text{ cm}^{-1}$ ) at  $\Phi = 5 \times 10^{20}$  photon  $\text{cm}^{-2} \text{s}^{-1}$  for sample C and 0.56 dB/cm ( $0.13 \text{ cm}^{-1}$ ) at  $\Phi = 1 \times 10^{21}$  photon  $\text{cm}^{-2} \text{s}^{-1}$  for sample D. These values are significantly higher than the 0.2 dB/cm found in sample B at similar  $\Phi$ .<sup>13)</sup> It has also to be noted that in sample B it is possible to achieve an internal gain of 0.6 dB/cm (comparable to the other samples) at a higher  $\Phi$  of about  $10^{22}$  photon  $\text{cm}^{-2} \text{s}^{-1}$ .

Since  $g = \sigma_{em} N_2 \Gamma$  and the absorption coefficient  $\alpha = \sigma_{abs} N_{Er} \Gamma$ , then

$$\frac{g}{\alpha} = \frac{\sigma_{em} N_2}{\sigma_{abs} N_{Er}} \approx \frac{N_2}{N_{Er}} \quad (10)$$

by assuming that at 1535 nm  $\sigma_{em} = \sigma_{abs}$ .<sup>26)</sup> Thus, we can estimate the percentage of  $Er^{3+}$  ions in the excited state. It results about 11, 9, and 7% of the total active erbium population for samples B, C, and D, respectively. These low inversion fractions are mainly due to a low population of  $Er^{3+}$  ions coupled to Si-nc, actually less than 3% of the Er content is coupled to Si-nc in these samples,<sup>23)</sup> being the rest excitable only through direct pumping.

Quantitative measurements of the photon flux emitted from these samples have allowed us to determine the number of  $Er^{3+}$  ions that are emitting as a function of  $\Phi$ .<sup>28)</sup> For example, in sample B, at emission saturation (high pumping  $\Phi$ ),  $N_2 \cong 3 \times 10^{19}$  ions  $cm^{-3}$ . From eq. (10), we found that  $N_2/N_{Er} = 11\%$ , thus it results that  $N_{Er} \cong 3 \times 10^{20}$  ions  $cm^{-3}$ , which fits quite well with the Er content determined by RBS (about  $4 \times 10^{20}$  ions  $cm^{-3}$ ). This evidences that all the Er deposited in the sample is optically active.

The partial inversion of  $Er^{3+}$  is confirmed also by the spectral dependence of SE. Figure 8 reports the data of sample D at  $\Phi = 1 \times 10^{21}$  photon  $cm^{-2} s^{-1}$  as a function of the probe wavelength. As it was observed for EDFA, partial inversion is observed as a signal enhancement which is larger than 1 at short wavelengths and smaller than 1 at longer wavelengths.<sup>33)</sup> In addition, the spectrum is distorted by the CA losses which depend quadratically on the wavelength as it is well established for bulk silicon,<sup>35,36)</sup> i.e., CA reduces more the probe photon flux for longer wavelengths.

It is interesting to compare the  $\sigma_{exc}$  measured at low  $\Phi$  (Fig. 4) with those extracted from the SE at high  $\Phi$ . Considering that all  $Er^{3+}$  ions are optically active as previously demonstrated, and using the approximation  $1/\tau_d(\Phi) = 1/\tau_d(\Phi \approx 0) + C_{up} N_2(\Phi, t = 0)$  to account for cooperative up-conversion, eq. (9) for samples C and D yields  $\sigma_{exc} \cong 6 \times 10^{-20} cm^2$  at  $\Phi = 1.4 \times 10^{21}$  photon  $cm^{-2} s^{-1}$  and  $\sigma_{exc} = 1 \times 10^{-20} cm^2$  for sample B at a similar photon flux

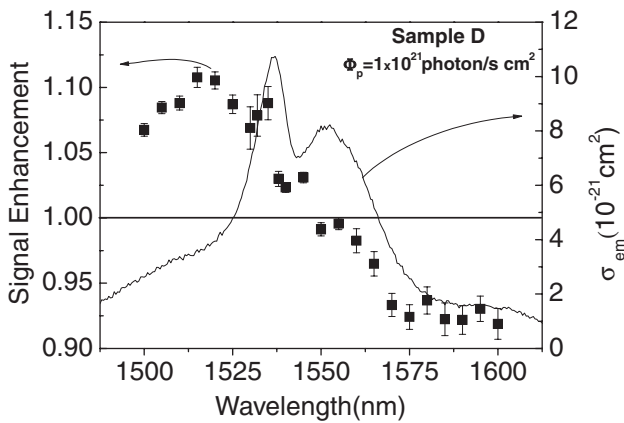


Fig. 8. Mean value of the signal enhancement (points) for different probe wavelengths at a fixed pump flux of  $1 \times 10^{21}$  photon  $cm^{-2} s^{-1}$ . The pump wavelength was 532 nm. The line refers to the emission cross section spectrum.

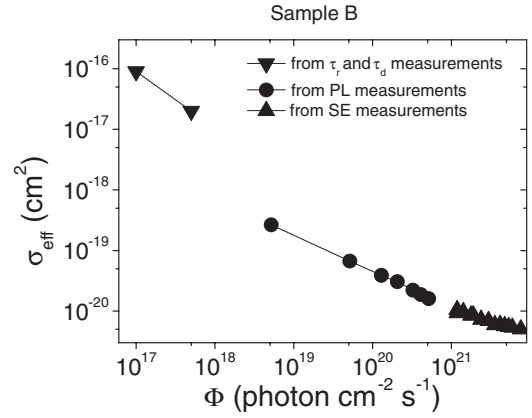


Fig. 9. Effective excitation cross-section of  $Er^{3+}$  as a function of the incident flux extracted from lifetime measurements (inverted triangles), from quantitative measurements of the density of excited  $Er^{3+}$  ions (circles) and from SE measurements (triangles). The pump wavelength is 488 nm, while the probe wavelength in the region of high pump photon flux was 1535 nm.

density. These values are similar to  $\sigma_{abs}$  for direct excitation of  $Er^{3+}$ , which means that most of the erbium is excited at high  $\Phi$  by direct internal absorption. Sample B shows lower  $\sigma_{exc}$  than the other two samples that show similar values. Several causes are responsible for this: CA turns off the excitation of  $Er^{3+}$  via Si-nc in a stronger way for sample B than for the others, as it was shown in Fig. 6; in addition, the absorption cross section is smaller in sample B than in the others (Fig. 2 and ref. 18). At low  $\Phi$  we are measuring orders of magnitude higher effective cross sections because most of the PL signal is coming from  $Er^{3+}$  excited via transfer from the Si-nc, as previously discussed.

Figure 9 reports the  $\sigma_{exc}$  obtained from SE data as a function of  $\Phi$  for sample B.  $\sigma_{exc}$  values for low  $\Phi$  ( $10^{17}$  photon  $cm^{-2} s^{-1}$ ) are extracted from lifetime measurements, for intermediate  $\Phi$  ( $10^{18}$ – $10^{20}$  photon  $cm^{-2} s^{-1}$ ) from quantitative measurements of the absolute amount of excited  $Er^{3+}$ , and for high  $\Phi$  ( $10^{21}$ – $10^{22}$  photon  $cm^{-2} s^{-1}$ ) from SE measurements. The main result is that  $\sigma_{exc}$  decreases with  $\Phi$  several orders of magnitude in the range of studied pump photon fluxes. This trend is compatible to what shown in Fig. 4 for low  $\Phi$ . The  $\sigma_{exc}$  reduction is due to the cumulative effects of an  $Er^{3+}$ –Si-nc distance dependence and of a reduction of the transfer rate from the Si-nc to  $Er^{3+}$  because of confined carrier absorption.

## 7. Conclusions

We have demonstrated that a reduction of the annealing time, while keeping constant all the other processing parameters, has significantly improved the Si-nc and  $Er^{3+}$  system by reducing the contribution of confined carrier absorption at high pump powers and increasing the emission cross section. This leads to a higher signal enhancement for lower pumping rate, which is a preferred result for application of the system in waveguide amplifiers. The reduced annealing time affects mainly the quality of the silica matrix in terms of reconstruction of the network yielding defected silica in which small Si-nc form. A larger up-conversion coefficient has been also observed for the short annealed samples, which translates into a shorter  $Er^{3+}$

lifetime. In this respect, a matrix of poor quality seems to favor the dimerization of the  $\text{Er}^{3+}$  ions and hence the phenomenon of up-conversion.

In any case, the main problem limiting the achievement of a net overall gain in the waveguide amplifier is lying in the few percentage of the erbium population that can be excited through the Si-nc and, hence, restricting the advantage of the properties of the coupled system. In addition, a flux dependent effective excitation cross section has been demonstrated due to the distance dependent coupling coefficient. Higher flux yields lower excitation cross section due to the saturation of the strongly coupled ions. Thus, the main problem to obtain overall gain with this system concerns the nanoengineering of the material composition allowing the production of materials with a high density of small sized Si-nc coupled effectively to all the  $\text{Er}^{3+}$  in the system. The small size is needed to minimize the CA, while the high density is necessary to increase the coupling with  $\text{Er}^{3+}$ .

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